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# A STUDY ON MHD JEFFREY FLUID FLOW PAST A VERTICAL POROUS PLATE WITH MULTIPLE BOUNDARIES UNDER THE EFFECT OF CHEMICAL REACTION

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Abstract: In non-Newtonian fluid flow Jeffrey fluid is the one which describes stress relaxation very well. This paper is mainly focused on analytical investigation of unsteady heat and mass transfer rate through porous medium in the presence of magnetic field along with radiation/absorption, heat generation/ absorption and homogeneous chemical reaction effects. The coupled linear partial differential equations are turned to ordinary equations by super imposing solutions with steady and time dependent transient part. Finally, the set of ordinary differential equations are solved with a perturbation method to meet the inadequacy of boundary condition. The effect of different parameters on the flow is described with the help of graphs and tables. This investigation is the fluctuation of velocity appears near the plate due to the presence of sink and presences of elastic element as well heat source reduces the skin friction. Impact of Jeffery parameter leads to decrease the fluid velocity. The heavier species with low conductivity reduces the flow within the boundary layer.

Keywords and Phrases: Porous plate, Thermal radiation, Chemical reaction, Heat and mass transfer, Jeffery fluid, thermal radiation, Grashof Number, MHD.
2020 Mathematics Subject Classification: 35Q35, 65L12, 76N20, 80M15.

### 1. Introduction

In the view of global wide various manufacturing and processing industries, there is a continuous effort in research for reducing or eliminating the hazards or harmful effects due to chemical reactions occurred, when the presence of foreign material in the chemical fluid flows. This makes the essential need to investigate the heat and mass transfer characteristics of chemical fluid flows. An important class of two-dimensional time dependent flow problem dealing with the response of boundary layer to external unsteady fluctuations of the free stream velocity about a mean value attracted the attention of many researchers. Besides, the convective flow through porous medium has applications in geothermal energy recovery, thermal energy storage, oil extraction, and flow through filtering devices. Now a days Magneto hydrodynamics is very much attracting the attention of the many authors due to its applications in geophysics and engineering. MHD flow with heat and mass transfer has been a subject of interest of many researchers because of its varied application in science and technology. Such phenomena are observed buoyancy induced motions in the atmosphere, in water bodies, quasi solid bodies such as earth, etc.

Hayat et al. [7-9] presented several aspects by investigating oscillatory rotating flows of a fractional Jeffrey fluid filling a porous space. Hussain et al. [10] examined radiative hydromagnetic flow of Jeffrey nanofluid by an exponentially stretching sheet. Santhosh et al. [15] noticed Jeffrey fluid flow through porous medium in the presence of magnetic field in narrow tubes. Shehzad et al. [16] observed the influence of thermophoretic and Joule heating on the radiative flow of Jeffrey fluid with mixed convection. Shehzad et al. [17] noticed MHD three-dimensional flow of Jeffrey fluid with Newtonian heating. Sreenath et al. [18-19] examined oscillatory flow of a conducting Jeffrey fluid in a composite porous medium channel. Several authors contributed in this area, to make a mention Kavitha et al. [11], Batti et al. [3], Krishna Murthy et al. [13]. Abu zeid et al. [1].

In the present investigation, the presence of radiation absorption and a transverse magnetic field is considered in an unsteady free convective flow of Jeffery fluid past an infinite vertical porous plate in a porous medium with time dependent oscillatory suction along with the permeability. This kind of environment is mostly present in various industries such as food processing firms, dairy industries, distilleries and beverage industries, polymer fabrication firms, glass manufacturing industries, pharmaceutical industries etc.

Kirubushankumar et al. [12] have examined that a Casson fluid flow and heat transfer over an unsteady porous stretching surface. Arthur et al. [2] have analyzed the Casson fluid flow over a vertical porous surface with a chemical reaction in the presence of a magnetic field. Pramanik [14] have studied that a Casson fluid flow and heat transfer past an exponentially porous stretching surface in the presence of thermal radiation. Vijay Kumar et al. [20] have investigated that Joule heating and thermal diffusion effects on MHD radiative and convective Casson fluid flow past an oscillating semi-infinite vertical porous plate. A. Hamid et.al [4] are analyzed the Characteristics of combined heat and mass transfer on mixed convection flow of Sisko fluid model. A. Hamid and M. Khan [5] are studied the Unsteady mixed convective flow of Williamson Nano fluid with heat transfer in the presence of variable thermal conductivity and magnetic. A.Hamid et al. [6] are given the Numerical simulation for heat transfer performance in unsteady flow of Williamson fluid driven by a wedge-geometry.

In the present investigation, the presence of radiation absorption and a transverse magnetic field is considered in an unsteady free convective flow of Jeffery fluid past an infinite vertical porous plate in a porous medium with time dependent oscillatory suction along with the permeability. This kind of environment is mostly present in various industries such as food processing firms, dairy industries, distilleries and beverage industries, polymer fabrication firms, glass manufacturing industries, pharmaceutical industries etc.

#### 2. Formulation and Problem

The unsteady free convective flow of a radiative, chemically reactive, heat absorbing, Casson fluid past an infinite vertical porous plate in a porous medium with time dependent oscillatory suction as well as permeability in presence of radiation absorption and a transverse magnetic field is considered. The schematic physical model of the analyzed problem is shown in Fig.2.1.



Figure 2.1: Physical model of the problem

The following assumption are made during the formulation of the problem and

those are;  $t^* < 0, v_0 > 0$  and  $\epsilon \leq 1$  are positive constants, Soret and Dofour effects are neglected. Let us consider the  $x^1$ -axis be along the plate in the direction of the flow and the  $y^1$ -axis normal to it. It is also considered that the magnetic Reynolds number is much less than unity so that induced magnetic field is neglected in comparison with the applied transverse magnetic field. The basic flow in the medium is, therefore, entirely due to the buoyancy force caused by the temperature difference between the wall and the medium. It is assumed that initially, at  $t^* < 0$ , the plate as well as fluids are at the same temperature and also concentration of the species is very low so that the Soret and Dofour effects are neglected. When  $t^*$ , the temperature of the plate is instantaneously raised to  $Tw^*$  and the concentration of the species is set to  $Cw^*$ . Let the permeability of the porous medium and the suction velocity be considered in the following forms respectively.

$$K^*(t^*) = K_p^*(1 + \epsilon e^{n^*t^*}), \nu^*(t^*) = -\nu_0(1 + \epsilon e^{n^*t^*}), \qquad (2.1)$$

where  $v_0 > 0$  and  $\epsilon \leq 1$  are positive constants. Under the above assumption with usual Boussinesq's approximation, the governing equations and boundary conditions are given by [Ref 11].

From the reference [11], the fluid selected for the present problem is Casson fluids instead of viscoelastic fluid. Also considered multiple boundaries in place of uniform boundary. Therefore the governing equations modified and obtained as equations (2.2) and (2.3) is

$$\frac{\partial u^*}{\partial t^*} = \left(\frac{1}{1+\beta}\right)\nu\frac{\partial^2 u^*}{\partial y^{*2}} + g\beta(T^* - T^*_\infty) + g\beta^*(C^* - C^*_\infty) - \sigma B_0^2\frac{u^*}{\rho} - \left(\frac{1}{1+\beta}\right)\nu\frac{u^*}{k^*}$$
(2.2)

$$\frac{\partial T^*}{\partial t^*}\rho c_p = K \frac{\partial^2 T^*}{\partial y^{*2}} - \frac{\partial q^*}{\partial y^*} - Q(T^* - T^*_\infty) + Q_l^*(C^* - C^*_\infty)$$
(2.3)

$$\frac{\partial C^*}{\partial t^*} = D \frac{\partial^2 C^*}{\partial y^{*2}} - K_r (C^* - C^*_\infty)$$
(2.4)

$$u = f(t) = 1, T^* = T_{\infty} + \epsilon (T_W - T_{\infty}) e^{i t}, C^* = C_{\infty} + \epsilon (C_W - C_{\infty}) e^{i t} \text{ at } y = 0$$
(2.5)

$$\begin{aligned} u \to 0, \ T^* \to T_{\infty}, \ C^* \to C_{\infty}, \ \text{as } y \to \infty. \\ y &= \frac{\nu_0 t^*}{\nu}, \ t = \frac{\nu_0^2 t^*}{4\nu}, \ w = \frac{4\vartheta\omega^*}{\nu_0^2}, \ u = \frac{u^*}{\nu_0}, \ T = \frac{T^* - T_{\infty}^*}{T_W - T_{\infty}}, \ C = \frac{C^* - C_{\infty}^*}{C_W - C_{\infty}}, \ K_c = \frac{k_r\nu}{\nu_0^2}, \\ P_r &= \frac{\nu}{K}, \ S = \frac{\vartheta S^*}{\nu_0^2}, \ K_p = \frac{\nu_0^2 K_p^2}{\nu^2}, \ M^2 = \sigma \frac{B_0^2 \nu}{\nu_0^2 \rho}, \ S_c = \frac{\nu}{D}, \ R = \frac{Q_l \nu (C_W^* - C_{\infty})}{\nu_0^2 \rho (T_W^* - T_{\infty})}, \ H = \frac{U_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 \rho}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2 V_0^2}{\nu_0^2 V_0^2 V_0^2 V_0^2 V_0^2}, \ M_s = \frac{U_0^2 V_0^$$

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$$F + S, \ G_c = \frac{\nu g \beta^* (C_W - C_\infty)}{\nu_0^3}, \ G_r = \frac{\nu g \beta^* (T_W - T_\infty)}{\nu_0^3}, \ F = \frac{4I_1 \nu}{\nu_0^2 \rho C_p}, \ s = \frac{Q \nu}{\nu_0^2 \rho C_p}, \ R_c = \frac{\nu_0^2 K_0}{\nu_0^2 \rho}$$
(2.6)

The equations (2.2)-(2.5) reduce to following non-dimensional form

$$\frac{1}{4}\frac{\partial u}{\partial t} = \left(\frac{1}{1+\beta}\right)\frac{\partial^2 u}{\partial y^2} + G_r T + G_c C - \left(M^2 + \frac{1}{K_p}\right)u \tag{2.7}$$

$$\frac{1}{4}\frac{\partial T}{\partial t} = \frac{1}{P_r}\frac{\partial^2 T}{\partial y^2} - HT + RC$$
(2.8)

$$\frac{1}{4}\frac{\partial C}{\partial t} = \frac{1}{S_c}\frac{\partial^2 C}{\partial y^2} - K_c C \tag{2.9}$$

$$u = f(t) = 1, T = 1 + \epsilon e^{nt}, C = 1 + \epsilon e^{nt} y = 0$$
(2.10)

$$u \to 0, T \to 0, C \to 0, \text{ as } y \to \infty.$$

# 3. Solution of the Problem

In view of periodic suction, temperature and concentration at the plate let us assume the velocity, temperature, concentration the neighborhood of the plate be

$$u(y,t) = u_0(y) + \epsilon e^{nt} u_1(y), T(y,t) = T_0(y) + \epsilon e^{nt} T_1(y), \text{ and } C(y,t) = C_0(y) + \epsilon e^{nt} C_1(y)$$
(3.1)

Substituting equations (3.1) into (2.7)-(2.9) and comparing the no harmonic and harmonic terms we get

$$\left(\frac{1}{1+\beta}\right)u_0^{11} - \left(M^2 + \frac{1}{K_p}\right)u_0 = -G_r T_0 - G_c C_0 \tag{3.2}$$

$$\left(\frac{1}{1+\beta}\right)u_1^{11} - \left(M^2 + \frac{1}{K_p} + \frac{n}{4}\right)u_1 = -G_cC_1 - G_rT_1 \tag{3.3}$$

$$T_0^{11} - P_r H T_0 = -R P_r C_0 (3.4)$$

$$T_1^{11} - \left(H + \frac{n}{4}\right)P_r T_1 = -RP_r C_1 \tag{3.5}$$

$$C_0^{11} - K_c S_c C_0 = 0 (3.6)$$

$$C_1^{11} - \left(K_c + \frac{n}{4}\right)S_cC_1 = 0 \tag{3.7}$$

The boundary conditions now reduce to

$$u_0 = 1, u_1 = 0, T_0 = T_1 = 1, C_0 = C_1 = 1, \text{ at } y = 0$$
  

$$u_0 = u_1 \to 0, T_0 = T_1 \to 0, C_0 = C_1 \to 0, \text{ as } y \to \infty$$
(3.8)

Solving these differential equations (3.2)-(3.8) with the help of boundary conditions we get,

$$u_1(y,t) = (t - b_3 - b_4)e^{-\sqrt{a_5}y} + b_3e^{-\sqrt{a_3}y} + b_4e^{-\sqrt{a_1}y} + \epsilon e^{nt} \left\{ (-b_5 - b_6)e^{-\sqrt{a_8}y} + b_5e^{-\sqrt{a_4}y} + b_6e^{-\sqrt{a_2}y} \right\}$$
(3.9)

$$u_{2}(y,t) = (\sin t - b_{3} - b_{4})e^{-\sqrt{a_{5}y}} + b_{3}e^{-\sqrt{a_{3}y}} + b_{4}e^{-\sqrt{a_{1}y}} + \epsilon e^{nt} \left\{ (-b_{5} - b_{6})e^{-\sqrt{a_{8}y}} + b_{5}e^{-\sqrt{a_{4}y}} + b_{6}e^{-\sqrt{a_{2}y}} \right\}$$
(3.10)

$$u_{3}(y,t) = (1 - b_{3} - b_{4})e^{-\sqrt{a_{5}}y} + b_{3}e^{-\sqrt{a_{3}}y} + b_{4}e^{-\sqrt{a_{1}}y} + \epsilon e^{nt} \left\{ (-b_{5} - b_{6})e^{-\sqrt{a_{8}}y} + b_{5}e^{-\sqrt{a_{4}}y} + b_{6}e^{-\sqrt{a_{2}}y} \right\}$$
(3.11)

$$T(y,t) = (1-b_1)e^{-\sqrt{a_3}y} + b_1e^{-\sqrt{a_1}y}\epsilon e^{nt} \left\{ (1-b_2)e^{-\sqrt{a_4}y} + b_2e^{-\sqrt{a_2}y} \right\}$$
(3.12)

$$C(y,t) = e^{-\sqrt{a_1}y} + \epsilon e^{nt} \left\{ e^{-\sqrt{a_2}y} \right\}$$
(3.13)

The skin friction at the plate in terms of amplitude and phase angle is given by

$$\tau = \frac{\partial u_0}{\partial y} + \epsilon e^{nt} \frac{\partial u_0}{\partial y} \quad \text{at} \quad y = 0$$
  
$$\tau = \left[ -(1 - b_3 - b_4)\sqrt{a_5} - b_3\sqrt{a_3} - b_4\sqrt{a_1} \right] + \epsilon e^{nt} \left[ (b_5 - b_6)\sqrt{a_8} - b_5\sqrt{a_4} - b_6\sqrt{a_2} \right]$$
(3.14)

The rate of heat transfer, i.e. heat flux at the  $N_u$  in terms of amplitude and phase is given by,

$$N_u = -\left[\frac{\partial T_0}{\partial y} + \epsilon e^{nt} \frac{\partial T_1}{\partial y}\right] \quad \text{at} \quad y = 0 \quad \text{is}$$
$$N_u = \left[(1 - b_3)\sqrt{a_3} + b_1\sqrt{a_1}\right] + \epsilon e^{nt} \left[(1 - b_2)\sqrt{a_4} + b_2\sqrt{a_2}\right] \tag{3.15}$$

The mass transfer coefficient, i.e., the Sherwood number  $(S_h)$  at the plate in terms of amplitude and phase is given by

$$S_h = -\left[\frac{\partial C_0}{\partial y} + \epsilon e^{nt} \frac{\partial C_1}{\partial y}\right] \quad \text{at} \quad y = 0 \quad \text{is} \quad S_h = \left[\sqrt{a_1}\right] + \epsilon e^{nt} \left[\sqrt{a_2}\right] \tag{3.16}$$

#### 4. Results and Discussions

In order to assess the effects of the dimensionless thermo physical parameters on the regime calculations have been carried out on velocity field, temperature field, and concentration field for various physical parameters like magnetic parameter, Prandtl parameter, Grashof number, modified Grashof number, chemical reaction parameter etc. The results are represented through graphs in figures 1 to 11. Figure 1, displays the velocity profiles for various values of magnetic parameter M. It is observed that the velocity decreases with an increase in M. This is due to fact that the applied magnetic field which acts as retarding force that condenses the momentum boundary layer. From figure 2, it displays that the velocity increases with an increase in Gc number. A similar effect is noticed from figure 3, in the presence of Schmidt number where velocity decreases. Figure 4, depicts the effects of Grashof number on velocity, from this figure it is noticed that the velocity increases with an increase in Gr. Influence of the  $m = \beta$  on velocity is presented in figure 5, from this figure it is noticed that the velocity decreases with an increase in Gr. Influence of the  $m = \beta$  on velocity is presented in figure 5, from this figure it is noticed that the velocity decreases with an increase in Kp. From figure 6, it is seen that the velocity increases with an increase in Kp. From figure 7 shows velocity increases for the increasing values of Prandtl number. Effect of radiation absorption is presented in figure 8, from this figure, it is noticed that the velocity decreases for increases in chemical reaction parameter. Effect of Schmidt number on temperature is shown in figure 10, which concludes that temperature decreases as the values of Sc increases. From figure 11, it is concluded that the concentration decreases as Kc increases.



Fig.1. Effect of M on Velocity

Fig.2. Effect of Gc of number on Velocity



Fig.3. Effect of Sc of number on Velocity Fig.4. Effect of Grashof number on Velocity



Fig.11. Effect of (Kc) on Concentration

Effects of various parameters on skin friction, the rate of heat transfer and also the rate of mass transfer are presented in tables 1-3. From table 1 it is noted that skin friction increases due to an increase in Grashof number Gr. But modified Grashof number has a different effect on skin friction. Skin friction decreases due to an increase in M. From this table it is also observed that the skin friction increases due to an increase in porosity parameter. From table 2 it is observed that skin friction increases for increasing values of R whereas Nusselt number decreases with the increasing values of R. Of course, skin friction, as well as Nusselt number increase for increasing values of Pr and also heat source parameter H. From table 3, it is found that skin friction and Sherwood number both increase for increasing values of Sc. whereas skin friction decreases with increase values of Kc, but a reverse effect is noticed in the case of Sherwood number.

#### Table.1: Effects of Gr,

#### Table .2: Effect of R and H

Table. 3: Effect of Sc and Kc on skin friction

Gc, M and Kp on skin

on skin friction coefficient

friction coefficient

and Nusselt number

and Sherwood number

Gr	Gc	М	Кр	Т	Γ
15	5	0.9	1.6	10.134	F
16	5	0.9	1.6	11.234	F
17	5	0.9	1.6	12.265	F
8	6	0.9	1.6	12.354	F
8	7	0.9	1.6	11.975	F
8	6	0.9	1.6	10.674	F
8	5	1.5	1.6	12.765	F
8	5	2.0	1.6	12.245	F
8	5	2.5	1.6	11.345	ſ
8	5	0.9	0.4	8.896	ſ
8	5	0.9	0.7	9.476	
0	5	0.0	0.0	0.706	

	R	Pr	н	Т	Nu
1	2	0.71	2	98.456	0.567
1	3	0.71	2	127.234	0.445
5	4	0.71	2	180.523	0.345
1	5	0.71	2	230.546	0.256
5	1.6	1.71	2	14.765	2.457
1	1.6	2.71	2	21.853	2.542
5	1.6	3.71	2	32.234	2.643
5	1.6	4.71	2	37.976	2.756
5	1.6	0.71	3	7.456	1.635
	1.6	0.71	4	8.456	1.845
	1.6	0.71	5	9.345	1.936
	1.6	0.71	6	11.897	2.345

Sc	Kc	Т	Sh
1.44	3	11.456	3.345
2.44	3	12.987	4.667
3.44	3	13.956	5.345
4.44	3	14.865	6.556
0.44	6	73.675	1.345
0.44	7	54.543	1.498
0.44	8	43.654	1.687
0.44	9	23.643	1.878

## 5. Conclusions

The following inferences are observed from the present investigation of unsteady MHD free convection flow of a Jeffery, incompressible, electrically conducting fluid past a vertical porous plate through a porous medium with time dependent oscillatory permeability and suction in presence of a uniform transverse magnetic field.

- The heavier species with low conductivity reduces the flow within the boundary layer.
- An increase in elasticity of the fluid leads to decrease the velocity which is an established result.
- Impact of Jeffery parameter leads to decrease the fluid velocity.

#### References

- Abu zeid M., Ali Khalid K., Shaalan M. A., Raslan K. R., Numerical study of thermal radiation and mass transfer effects on free convection flow over a moving vertical porous plate using cubic B-spline collocation method, Journal of the Egyptian Mathematical Society, 27(36) (2019), 1-17.
- [2] Arthur E. M., Seini I. Y. and Bortteir L. B., Analysis of Casson fluid flow over a vertical porous surface with a chemical reaction in the presence of a magnetic field, Journal of Applied mathematics and Physics, 3(06), (2015), 713.
- [3] Bhatti M. M., Ali Abbas M., Simultaneous effects of slip and MHD on peristaltic blood flow of Jeffrey fluid model through a porous medium, Alexandr Eng J, 55 (2016), 1017-1023.
- [4] Hamid A. et.al, Characteristics of combined heat and mass transfer on mixed convection flow of Sisko fluid model: A numerical study, Modern Physics Letters B, 34 (24), (2020), 250-255.
- [5] Hamid A. and Khan M., Unsteady mixed convective flow of Williamson nanofluid with heat transfer in the presence of variable thermal conductivity and magnetic, Journal of Molecular Liquids, 260 (2018), 436-446.
- [6] Hamid A., Hashim, Khan M., Numerical simulation for heat transfer performance in unsteady flow of Williamson fluid driven by a wedge-geometry, Results in Physics, 9 (2018), 479-485.
- [7] Hayat T., Khan M., Fakhar K., and Amin N., Oscillatory Rotating Flows of a Fractional Jeffrey Fluid Filling a Porous Space, Frontiers in Heat and Mass Transfer (FHMT), 10 (2018), 25.

- [8] Hayat T., Mustafa M., and Naturforsch Z., The Effect of Thermal Radiation on the Unsteady Mixed Convection Flow of a Jeffrey Fluid Past a Porous Vertical Stretching Surface Using Homotopy Analysis Method (HAM), 65a (2010), 711-719.
- [9] Hayat T., Shehzad S. A., Qasim M. and Obaidat S., Radiative Flow of Jeffery Fluid in a Porous Medium with Power Law Heat Flux and Heat Source, Nucl. Eng, 243 (2012), 15–19.
- [10] Hussain T., Shehzad S. A., Hayat T., Alsaedi A., Al-Solamy F. and Ramzan M., Radiative Hydromagnetic Flow of Jeffrey Nanofluid by an Exponentially Stretching Sheet, Plos One, 9(8) (2014), 1-9.
- [11] Kavita K., Prasad K. Ramakrishna, Aruna Kumari B., Influence of heat transfer on MHD oscillatory flow of Jeffrey fluid in a channel, Adv Appl Sci Res, 3 (2012), 2312-2325.
- [12] Kirubhashankar C. K., Ganesh S. and Ismail A. M., Casson fluid flow and heat transfer over an unsteady porous stretching surface, Applied Mathematical Sciences, 9(7), (2015), 345-351.
- [13] Murthy M. Krishna, Couette M. H. D., Flow of Jeffrey fluid in a porous channel with heat source and chemical reaction, Middle-East J Scient Res, 24 (2016), 585-592.
- [14] Pramanik S., Casson fluid flow and heat transfer past an exponentially porous stretching surface in the presence of thermal radiation, Ain Shams Engineering Journal, 5(1), (2014), 205-212.
- [15] Santhosh N. and Radhakrishnamacharya D., Jeffrey Fluid Flow through Porous Medium in the Presence of Magnetic Field in Narrow Tubes, Hindawi Publishing Corporation, International Journal of Engineering Mathematics Article, (2014), 1-8.
- [16] Shehzad S. A., Alsaedi A., and Hayat T., Influence of Thermophoresis and Joule Heating on the Radiative Flow of Jeffrey Fluid with Mixed Convection, Braz. J. Chem. Eng., 30(4) (2013), 897-908.
- [17] Shehzad S. A., Hayat T., Alhuthali M. S. and Asghar S., MHD Three-Dimensional Flow of Jeffrey Fluid with Newtonian Heating, J. Cent. South Univ., 21 (2014), 1428-1433.

- [18] Sreenadh S., Prakash J., Parandhama A. and Ravi Kumar Y. V. K., Oscillatory Flow of a Conducting Jeffrey Fluid in a Composite Porous Medium Channel, 10th International Conference on Heat Transfer, Fluid Mechanics and Thermodynamics, 14-16 (2014), Florida, 2350-2358.
- [19] Sreenadh S., Rashidi M. M., Naidu K. Kumara Swamy and Parandhama A., Free Convection Flow of a Jeffrey Fluid through a Vertical Deformable Porous Stratum, Journal of Applied Fluid Mechanics, 9(5), (2016), 2391-2401.
- [20] Vijaya Kumar A. G., Veeresh C., Varma S. V. K., Umamaheswar M. and Raju M. C., Joule heating and thermal diffusion effects on MHD radiative and convective Casson fluid flow past an oscillating semi-infinite vertical porous plate, Frontiers in Heat and Mass Transfer (FHMT), 8 (2017), 1-8.