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## STUDY ON LORENTZIAN PARA-KENMOSTU MANIFOLDS ADMITTING GENERALIZED TANAKA-WEBSTER CONNECTION

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**Abstract:** In this study, we analyze the curvature properties and Ricci solitons in Lorentzian para-Kenmotsu manifolds using the generalized Tanaka-Webster connection. Here, using a generalized Tanaka-Webster connection, we examine the recurring conditions of the Lorentzian para-Kenmotsu manifold, projective curvature tensor, and conharmonic curvature tensor. Furthermore, using a generalized Tanaka-Webster connection, we investigate Ricci solitons on Lorentzian para-Kenmotsu manifolds.

Keywords and Phrases: Lorentzian para-Kenmotsu Manifold, Generalized Tanaka - Webster connection,  $\phi$ -recurrent, Ricci-solitons.

2020 Mathematics Subject Classification: 53C05, 53C07, 53C50.

## 1. Introduction, Notations and Definitions

On a non-degenerate pseudo-Hermitian CR-manifold, the Tanaka-Webster connection is a canonical affine connection [18, 21]. For contact metric manifolds, Tanno [19] defined the generalized Tanaka-Webster connection via the canonical connection, which is equivalent to the Tanaka-Webster connection provided that the corresponding CR-structure is integrable. Numerous writers have recently examined the generalized Tanaka-Webster link in Kenmotsu manifolds [5, 13, 15].