South East Asian J. of Mathematics and Mathematical Sciences Vol. 19, No. 3 (2023), pp. 319-332 DOI: 10.56827/SEAJMMS.2023.1903.25 ISSN (Onli

ISSN (Online): 2582-0850 ISSN (Print): 0972-7752

## CONJUGATE S<sub>3</sub>-MAGIC GRAPHS

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(Received: Apr. 20, 2023 Accepted: Dec. 10, 2023 Published: Dec. 30, 2023)

Abstract: In this paper, we introduce conjugate A-magic labeling of graphs where A is a finite non-abelian group and investigate the graphs that are conjugate  $S_3$ -magic.

Keywords and Phrases: A-magic labeling, Non-abelian group, conjugate  $S_3$ -magic.

## 2020 Mathematics Subject Classification: 05C25, 05C78.

## 1. Introduction

Throughout this paper, we shall consider only connected, finite, simple, and undirected graphs. Let G = (V(G), E(G)) be any finite graph and let A be an abelian group under addition with the identity element 0. Let  $A^* = A \setminus \{0\}$ . Any mapping  $\ell : E(G) \to A^*$  is called an edge labeling. Observe that any edge labeling induces a mapping  $\ell^+ : V(G) \to A$  as follows:  $\ell^+(u) = \Sigma\{\ell(uv) : uv \in E(G)\}$ . A graph G is called A-magic, if there exists  $a \in A$  such that  $\ell^+(u) = a$ , for all  $u \in V(G)$ . Several authors studied about  $V_4$ -magic graphs [6, 8, 9] and  $Z_k$ magic graphs [5]. Recently, Anusha C. and Anil Kumar V. [2, 3, 4] introduced A-magic labeling of graphs where A is non-abelian and studied graphs that are  $S_3$ magic,  $D_4$ -magic and  $Q_8$ -magic. In this paper, we introduce a new magic labeling of graphs using a non-abelian group namely, the conjugate A-magic labeling of graphs and investigate conjugate  $S_3$ -magic labeling of some graphs. Consider the set  $X = \{1, 2, 3\}$ . A permutation of X is a function from X to itself that is both