

## EDGE ITALIAN DOMINATION OF SOME GRAPH PRODUCTS

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**Abstract:** An edge Italian dominating function (EIDF) of a graph  $G = (V, E)$  is a function  $f : E(G) \rightarrow \{0, 1, 2\}$  such that every edge  $x$  with  $f(x) = 0$  is adjacent to some edge  $y$  with  $f(y) = 2$  or adjacent to at least two edges  $z_1, z_2$  with  $f(z_1) = f(z_2) = 1$ . The weight of an edge Italian dominating function is the sum  $\sum_{x \in E(G)} f(x)$  and the minimum weight of an edge Italian dominating function of  $G$  is called the edge Italian domination number of  $G$  and is denoted by  $\gamma'_I(G)$ . In this paper, we determine the edge Italian domination number of some graph products.

**Keywords and Phrases:** Edge Italian Domination, Edge Italian dominating function, Edge Italian Domination number.

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### 1. Introduction

Let  $G = (V, E)$  be a simple connected graph with vertex set  $V = V(G)$  and edge set  $E = E(G)$ . A graph  $G$  with  $p$  vertices and  $q$  edges will be referred to as a  $(p, q)$ -graph. A subset  $S$  of  $V$  is called a dominating set of  $G$  if every vertex not in  $S$  is adjacent to some vertex in  $S$ . The domination number,  $\gamma(G)$ , of  $G$  is the minimum cardinality taken over all dominating sets of  $G$ . The concept of edge domination in graphs was introduced by Mitchell and Hedetniemi [6]. A subset  $F$  of edges of a graph  $G$  is called an edge dominating set of  $G$  if every edge not in