South East Asian J. of Mathematics and Mathematical Sciences Vol. 19, No. 2 (2023), pp. 331-344

DOI: 10.56827/SEAJMMS.2023.1902.25

ISSN (Online): 2582-0850

ISSN (Print): 0972-7752

## IN $M_v^b$ - COMPLETE METRIC SPACE, COMMON FIXED POINT THEOREMS FOR TWO AND FOUR SELF-MAPS UNDER DIFFERENT CONTRACTION PRINCIPLES

Thakur Durga Bai and Rangamma Manchala

Department of Mathematics, Osmania University, Hyderabad - 500007, Telangana, INDIA

E-mail : durgabaithakur@rediffmail.com

(Received: Mar. 05, 2023 Accepted: Jul. 22, 2023 Published: Aug. 30, 2023)

Abstract: Two distinct theorems are presented in this manuscript. The first one establishes the existence of coincidence points and the *g*-weakness of  $M_v^b$  metric space. The Reich contraction principle produces a unique common fixed point for two maps, as illustrated in various examples. Second, same concept is used to identify common fixed point for four self maps. The Kannan and Banach contraction principles were applied in conjunction with extra requirements to get the fixed points as corollaries. This theorem's approach was used to solve several examples.

**Keywords and Phrases:** Fixed point, self maps, Complete  $M_v^b$  metric space,  $m_v^b$ -convergent, coincidence point.

2020 Mathematics Subject Classification: 47H10, 54H25.

## 1. Introduction and Preliminaries

Many academics have tried to generalize and enlarge metric spaces. Take a non-empty set M and distance function  $d: M \times M \to \mathbb{R}^+$ . Pick any x, y, z in M. The pair (M, d) is a metric space if it satisfies  $d(x, y) = 0 \Leftrightarrow x = y; d(x, y) =$  $d(y, x); d(x, y) \leq d(x, z) + d(z, y)$ . For example Mitrovic' and Radenovic' [7], Karahan and Isik [4], and Asim et al. [1] suggested the  $b_v(s)$ - metric,  $p_v^b$ - metric, and  $M_v$ - metric spaces. The generalization of  $b_v(s)$ -- metric,  $p_v^b$ - metric, and  $M_v$  - metric spaces is  $M_v^b$ - metric space, introduced by Joshi et al. [3] in 2021.  $M_v^b$ - metric