

A SUBCLASS OF HARMONIC FUNCTIONS DEFINED BY A CERTAIN FRACTIONAL CALCULUS OPERATORS

Jitendra Awasthi

Department of Mathematics,
S. J. N. M. P. G. College,
Lucknow - 226001, Uttar Pradesh, INDIA

E-mail : drjitendraawasthi@gmail.com

(Received: Feb. 16, 2022 Accepted: Apr. 18, 2023 Published: Apr. 30, 2023)

Abstract: In this paper a subclass of p -valent harmonic functions in the open unit disc is introduced by making use of a certain fractional calculus operator and some properties such as coefficient estimates, distortion theorem and extreme points are studied.

Keywords and Phrases: Open Unit disk, Multivalent Functions, Harmonic Functions.

2020 Mathematics Subject Classification: 30C45, 30A20, 34A40.

1. Introduction

A continuous function $f = u + iv$ is a complex valued harmonic function in a complex domain C , if both u and v are real harmonic in C . In any simply connected domain $D \subseteq C$, we can write $f = h + \bar{g}$. We call h the analytic part and g the co-analytic part of f . A necessary and sufficient condition for f to be locally univalent and sense-preserving in D is that $|h'(z)| > |g'(z)|$ in D (see Clunie and Sheil-Small [3]).

Denote by $M(p)$ the class of functions $f = h + \bar{g}$, that are harmonic multivalent and sense-preserving in the unit disk $U = \{z \in C : |z| < 1\}$. The class $M(p)$ was studied by Ahuja and Jahangiri [1] and class $M(p)$ for $p=1$ was defined and studied by Jahangiri et. al. in [5]. For $f = h + \bar{g} \in M(p)$, we may express the analytic functions