

ON ALAN DAY'S DOUBLING CONSTRUCTION IN  
BOOLEAN ALGEBRA

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(Received: Aug. 08, 2021 Accepted: Oct. 01, 2021 Published: Nov. 30, 2021)

Special Issue

Proceedings of International Virtual Conference on  
"Mathematical Modelling, Analysis and Computing IC- MMAC- 2021"

**Abstract:** In this paper, we prove that in a Boolean Algebra, doubling of an interval makes it distributive but not Boolean.

**Keywords and Phrases:** Lattices, boolean algebra, doubling construction in lattices.

**2020 Mathematics Subject Classification:** 44A99.

### 1. Introduction

G. Grätzer in his paper [4] introduced a new lattice  $L^U$  from a given lattice  $L$  by adding an element  $a^U$  called the double of  $a \neq 0, 1$  in  $L$  where  $L^U = L \cup \{a^U\}$  with a new order denoted by  $\leq^U$ . Following that construction, A. Day [1] introduced a similar construction  $L[I]$  by doubling an interval  $I$  of a given lattice  $L$ . After that it witnessed many developments, e.g. see [2], [3], [6]. In the paper [3] entitled 'Doubling Constructions in Lattice Theory', Alan Day mentioned the following result which appeared in [2]: Let  $L$  be a distributive lattice and take  $I = [u, v]$  in  $L$ ,  $L[I]$  is again distributive if and only if  $L = [u, 1] \cup [0, v]$ . The proof there is implicit. For Boolean algebras, we give in this paper an explicit proof.