

**BILINEAR CONCOMITANT AND GREEN'S FORMULA  
ASSOCIATED WITH A MATRIX DIFFERENTIAL OPERATOR**

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**Abstract:** In this paper, we have considered a matrix differential operator and the corresponding eigenvalue problem. The bilinear concomitant for the problem has been obtained. After this, the Lagrange's Identity and the Green's Formula has been derived.

**Keywords and Phrases:** Matrix differential operator, eigenvalue, bilinear concomitant, Lagrange's Identity, Green's Formula.

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**1. Introduction**

The differential equation, which is considered in the problem, is given below,

$$\begin{aligned} -\frac{d}{dx} \left( P_0 \frac{du}{dx} \right) + pu + rv &= \lambda(F_{11}u + F_{12}v) \\ i \frac{dv}{dx} + qv + ru &= -\lambda(F_{21}u + F_{22}v) \end{aligned} \tag{1}$$

where,

- (i)  $P_0$  is a real valued function of  $u$ , having continuous derivatives of the first order in  $a \leq x \leq b$ .
- (ii)  $p, q, r$  are all real valued function of  $u$  continuous in  $a \leq x \leq s$ .