

**PERTURBATION OF INFINITESIMAL GENERATOR IN  
SEMIGROUP OF LINEAR OPERATOR**

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**Abstract:** This paper consists of results on contraction semigroups thereby considering  $\omega$ -order reversing partial contraction mapping (semigroup of linear operator) as the infinitesimal generator of the semigroup on perturbation by bounded linear operators which we will show that the addition of a bounded linear operator  $B$  to an infinitesimal generator  $A$  of a semigroup of linear operator does not destroy the property of  $A$ .

**Keywords and Phrases:**  $\omega$ -ORCP $_n$ ,  $C_0$ -Semigroup, Contraction Semigroup, Perturbation.

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### 1. Introduction

Let  $X$  be a Banach space,  $X_n \subseteq X$  be a finite set,  $(T(t))_{t \geq 0}$  the  $C_0$ -semigroup,  $\omega$ -ORCP $_n$  be  $\omega$ -order-reversing partial contraction mapping which is an example of  $C_0$ -semigroup,  $\omega$ -ORCP $_n \subseteq$  ORCP $_n$  (Order Reversing Partial Contraction Mapping). Let  $M_m(\mathbb{N} \cup 0)$  be a matrix,  $L(X)$  the bounded linear operator in  $X$ ,  $P_n$ , the partial transformation semigroup,  $\rho(A)$  a resolvent of  $A$ , where  $A$  is the infinitesimal generator of a semigroup of linear operator and  $F(x)$  be a duality