J. of Ramanujan Society of Mathematics and Mathematical Sciences Vol. 9, No. 1 (2021), pp. 11-28

ISSN (Online): 2582-5461

ISSN (Print): 2319-1023

## ON SOME GROWTH PROPERTIES OF COMPOSITE ENTIRE FUNCTIONS ON THE BASIS OF THEIR GENERALIZED RELATIVE ORDER $(\alpha, \beta)$

## Tanmay Biswas and Chinmay Biswas\*

Rajbari, Rabindrapally, R. N. Tagore Road, P.O. Krishnagar, Nadia - 741101, West Bengal, INDIA

E-mail: tanmaybiswas\_math@rediffmail.com

\*Department of Mathematics, Nabadwip Vidyasagar College, Nabadwip, Nadia - 741302, West Bengal, INDIA

E-mail: chinmay.shib@gmail.com

(Received: Sep. 22, 2021 Accepted: Nov. 18, 2021 Published: Dec. 30, 2021)

**Abstract:** In this paper we wish to investigate some interesting results associated with the comparative growth properties of composite entire functions using generalized relative order  $(\alpha, \beta)$  and generalized relative lower order  $(\alpha, \beta)$ , where  $\alpha$  and  $\beta$  are continuous non-negative functions defined on  $(-\infty, +\infty)$ .

**Keywords and Phrases:** Entire function, growth, composition, generalized relative order  $(\alpha, \beta)$ , generalized relative lower order  $(\alpha, \beta)$ .

2020 Mathematics Subject Classification: 30D35, 30D30, 30D20.

## 1. Introduction, Definitions and Notations

Let  $\mathbb C$  be the set of all finite complex numbers and f be an entire function defined on  $\mathbb C$ . The maximum modulus function  $M_f(r)$  and the maximum term  $\mu_f(r)$  of  $f = \sum_{n=0}^\infty a_n z^n$  on |z| = r are defined as  $M_f = \max_{|z|=r} |f(z)|$  and  $\mu_f(r) = \max_{n\geq 0} (|a_n|r^n)$  respectively. Since  $M_f(r)$  is strictly increasing and continuous, therefore there exists its inverse function  $M_f^{-1}: (|f(0)|, \infty) \to (0, \infty)$  with  $\lim_{s\to\infty} M_f^{-1}(s) = \infty$ . We