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ON RAMANUJAN'S TAU-FUNCTION

J. López-Bonilla, S. Vidal-Beltrán, R. Rajendra* and
P. Siva Kota Reddy**

ESIME-Zacatenco

Instituto Politécnico Nacional

Edif. 4, 1er. Piso, Col. Lindavista CP 07738, CDMX, MEXICO

E-mail : jlopezb@ipn.mx, svidalb@ipn.mx

*Department of Mathematics

Field Marshal K. M. Cariappa College, Madikeri - 571201, INDIA

E-mail : rrajendrar@gmail.com

**Department of Mathematics

JSS Science and Technology University, Mysuru - 570006, INDIA

E-mail : pskreddy@jssstuniv.in

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Abstract: We exhibit a recurrence relation for the Ramanujan's tau-function involving the sum of divisors function, whose solution gives a closed formula for $\tau(n)$ in terms of complete Bell polynomials. Besides, we show that it is possible to write $\tau(n)$ in terms of the compositions of n .

Keywords and Phrases: Z-transform, Sum of divisors function, Recurrence relations, Ramanujan's function $\tau(n)$, Complete Bell polynomials, Color partitions, Compositions.

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1. Introduction

We begin with the recurrence relation [1, 5, 6, 10, 20, 25, 30, 37]:

$$np_k(n) = -k \sum_{j=1}^n \sigma(j) p_k(n-j), \quad n \geq 1, \quad (1)$$