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# ON SOFT CONTRA $g^*\beta$ -CONTINUOUS FUNCTIONS IN SOFT TOPOLOGICAL SPACES

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**Abstract:** We introduce a new class of soft contra generalized star beta continuous function (contra  $g^*\beta^s$ -conts function) in soft topological spaces. Also we present almost contra  $g^*\beta^s$ -continuous functions and we derive some basic properties.

Keywords and Phrases: Contra  $g^*\beta^s$ -continuous, almost contra  $g^*\beta^s$ -continuous, contra  $g^*\beta^s$ -irresolute.

2020 Mathematics Subject Classification: 54A40, 54C05, 54C10, 54C08.

## 1. Introduction

Initially the concept of generalized closed sets were introduced by Levine [3] in topological spaces in 1970. Molodtsov [4] pioneered the study of soft set theory as a new mathematical tool and confronted the fundamental results of the soft sets in 1996. Soft topological spaces(STS) are defined over an initial universe with a fixed set of parameters and was introduced by Munazza Naz & Muhammad Shabir [5]. The authors [6, 7] introduced the concept of generalized star  $\beta$ -closed sets in TS and soft  $g^*\beta$ -closed sets in STS. In this paper we introduced the new concept of contra  $g^*\beta^s$ -continuous function and contra  $g^*\beta^s$ -irresolute functions and we have discussed some properties. Also we present almost contra  $g^*\beta^s$ -continuous functions and we derive some of its characteristics and several properties are investigated. For the concepts of STS we refer [1, 2, 6, 7, 9].

### 2. Soft Contra $g^*\beta$ -Continuous Function

**Definition 2.1.** A function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is said to be soft contra  $g^*\beta$ -continuous, denoted by contra  $g^*\beta^s$ -conts function, if  $g^{-1}(F, \mathcal{K})$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$  for every soft open (briefly, open<sup>s</sup>)set  $(F, \mathcal{K})$  of  $(\mathcal{V}, \mu, \mathcal{K})$ .

#### Theorem 2.2.

- (a) Every soft contra conts is contra  $g^*\beta^s$  conts.
- (b) Every contra  $g^s$  conts is contra  $g^*\beta^s$  conts.
- (c) Every contra  $gs^s$  conts is contra  $g^*\beta^s$  conts.
- (d) Every contra  $\alpha^s$ -conts is contra  $g^*\beta^s$  conts.
- (e) Every contra  $g\alpha^s$ -conts is contra  $g^*\beta^s$  conts.
- (f) Every contra  $\pi g^s$ -conts is contra  $g^*\beta^s$  conts.
- (g) Every contra  $\pi gb^s$ -conts is contra  $g^*\beta^s$  conts.
- (h) Every contra  $\beta^s$  conts is contra  $g^*\beta^s$  conts.
- (i) Every contra  $g\beta^s$  conts is contra  $g^*\beta^s$  conts.
- (j) Every contra  $rg\beta^s$  conts is contra  $g^*\beta^s$  conts.

## Proof.

- (a) Let a function  $g: (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is soft contra conts and let  $(F, \mathcal{K})$  be a open<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Then  $g^{-1}(F, \mathcal{K})$  is closed<sup>s</sup> in  $(\mathcal{U}, \tau, E)$ . Because every closed<sup>s</sup> set is  $g^*\beta^s$ -closed, so  $g^{-1}(F, \mathcal{K})$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ . Therefore g is contra  $g^*\beta^s$ -conts.
- (b) Let a function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^{s}$  conts and let  $(F, \mathcal{K})$ be a open<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Then  $g^{-1}(F, \mathcal{K})$  is  $g^{s}$ - closed in  $(\mathcal{U}, \tau, E)$ . Because every  $g^{s}$ - closed set is  $g^{*}\beta^{s}$ -closed, so  $g^{-1}(F, \mathcal{K})$  is  $g^{*}\beta^{s}$ -closed in  $(\mathcal{U}, \tau, E)$ . Therefore q is contra  $q^{*}\beta^{s}$ -conts.

(c) Let a function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  contra  $gs^{s}$ - conts and let  $(F, \mathcal{K})$  be a open<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Then  $g^{-1}(F, \mathcal{K})$  is  $gs^{s}$ - closed in  $(\mathcal{U}, \tau, E)$ . Because every  $gs^{s}$ - closed set is  $g^{*}\beta^{s}$ -closed, so  $g^{-1}(F, \mathcal{K})$  is  $g^{*}\beta^{s}$ -closed in  $(\mathcal{U}, \tau, E)$ . Therefore g is contra  $g^{*}\beta^{s}$ -conts.

The proof will same for remaining.

**Example 2.3.** Make  $\mathcal{U} = \{p, q, r\} = \mathcal{V}, E = \{e_1, e_2\}.$ Let  $F_1, F_2, F_3, F_4, F_5, F_6, F_7$  are functions from E to  $P(\mathcal{U})$  and are defined as follows:  $F_1(e_1) = \{p\}, F_1(e_2) = \{p\}, F_2(e_1) = \{q\}, F_2(e_2) = \{q\}, F_3(e_1) = \{r\}, F_3(e_2) = \{p\}, F_4(e_1) = \{p, q\}, F_4(e_2) = \{p, q\}, F_5(e_1) = \{p, r\}, F_5(e_2) = \{p\}, F_6(e_1) = \{q, r\}, F_6(e_2) = \{q\}$ 

Then  $\tau = \{\Phi, \mathcal{U}, (F_1, E), \dots, (F_6, E)\}$  is a soft topology and elements in  $\tau$  are open<sup>s</sup> sets.

Let  $\mathcal{H}_1, \mathcal{H}_2, \mathcal{H}_3, \mathcal{H}_4, \mathcal{H}_5, \mathcal{H}_6$  are functions from E to  $P(\mathcal{K})$  and are defined as follows:  $\mathcal{H}_1(e_1) = \{r\}, \mathcal{H}_1(e_2) = \{q\}, \mathcal{H}_2(e_1) = \{r\}, \mathcal{H}_2(e_2) = \{p\}, \mathcal{H}_3(e_1) = \{r\}, \mathcal{H}_3(e_2) = \{q, p\}, \mathcal{H}_4(e_1) = \{p, r\}, \mathcal{H}_4(e_2) = \{p\}, \mathcal{H}_5(e_1) = \{r, p\}, \mathcal{H}_5(e_2) = \{q, p\}, \mathcal{H}_6(e_1) = \{p, r\}, \mathcal{H}_6(e_2) = \{q\}.$ 

So,  $\mu = \{\Phi, \mathcal{V}, (\mathcal{H}_1, E), \dots, (\mathcal{H}_6, E)\}$  is a soft topology on  $\mathcal{V}$ .

Defined an identity map  $g: \mathcal{U} \to \mathcal{V}$ . Now the inverse image of the open<sup>s</sup> set in  $(\mathcal{V}, \mu)$  is  $g^*\beta$ -closed. Then g is contra  $g^*\beta^s$ -conts.

Hence  $(\mathcal{S}, E) = \{\{p\}, \{p,q\}\}, \{\{p,r\}, \{p\}\}, \{\{p,q\}, \{q\}\}, \{\{p,r\}, \{p,q\}\} \text{ in } (\mathcal{V}, \mu) \text{ is closed}^s, g^s\text{-closed}, gs^s\text{-closed}, \alpha^s\text{- closed}, g\alpha^s\text{-closed}, \pi g^s\text{- closed}, \pi gb^s\text{-closed}, \beta^s\text{-closed}, g\beta^s\text{-closed}, \pi g\beta^s\text{-close}, \pi$ 

Therefore g is contra  $g^*\beta^s$ -conts is not soft contra conts, contra  $g^s$ - conts, contra  $gs^s$ - conts, contra  $g\alpha^s$ -conts, contra  $\pi g^s$ -conts, contra  $\pi gb^s$ -conts, contra  $\pi gb^s$ -conts, contra  $g\beta^s$ - conts, contra  $rg\beta^s$ - conts, contra  $rg\beta^s$ - conts.

**Theorem 2.4.** If  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  be a function is contra  $g^*\beta^s$ -conts and  $(\mathcal{H}, E)$  is open<sup>s</sup> in  $(\mathcal{U}, \tau, E)$ , then  $(g/\mathcal{H}) : (\mathcal{H}, \tau', E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts.

**Proof.** Consider  $(F, \mathcal{K})$  be soft closed in  $\mathcal{V}$ . Since  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts,  $g^{-1}(F, \mathcal{K})$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Then  $(g/\mathcal{H})^{-1}(F, \mathcal{K}) = g^{-1}((F, \mathcal{K}) \cap (\mathcal{H}, E))$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Therefore  $(g/\mathcal{H})^{-1}(F, \mathcal{K})$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ .

**Theorem 2.5.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  be a function, then the following are equivalent

(a) g is contra  $g^*\beta^s$ -conts.

b) For every closed<sup>s</sup> set  $(F, \mathcal{K})$  of  $(\mathcal{V}, \mu, \mathcal{K})$ ,  $g^{-1}(F, \mathcal{K})$   $g^*\beta^s$ -open.

**Proof.** Straightforward. Thus  $(a) \Leftrightarrow (b)$  is obvious.

**Definition 2.6.** A STS  $(\mathcal{U}, \tau, E)$  is said to be  $g^*\beta^s$ -locally indiscrete, denoted by  $g^*\beta^s$ - lc.indisc, if every  $g^*\beta^s$ -open is closed<sup>s</sup>.

**Theorem 2.7.** If a function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts and  $\mathcal{U}$  be a  $g^*\beta^s$ - lc.indisc, then g is soft contra conts.

**Proof.** Consider  $(\mathcal{S}, E)$  be open<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Then  $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$  -open in  $(\mathcal{U}, \tau, E)$ . Since  $\mathcal{U}$  is  $g^*\beta^s$ - lc.indisc,  $g^{-1}(\mathcal{S}, E)$  is closed in  $(\mathcal{U}, \tau, E)$ . Therefore g is soft contra continuous.

**Theorem 2.8.** If  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts and the space  $(\mathcal{U}, \tau, E)$  is  $g^*\beta^s$ -space then g is soft contra continuous.

**Proof.** Consider  $(\mathcal{S}, E)$  be open<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Since g is contra  $g^*\beta^s$ -conts,  $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Since  $\mathcal{U}$  is  $g^*\beta^s$ - space,  $g^{-1}(\mathcal{S}, E)$  is closed set in  $\mathcal{U}$ . Therefore g is soft contra continuous.

**Remark 2.9.** The composition of two contra  $g^*\beta^s$ -conts functions need not be contra  $g^*\beta^s$ -conts.

**Theorem 2.10.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is soft continuous then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -conts.

**Proof.** Let  $(\mathcal{S}, E)$  be open<sup>s</sup> in  $(\mathcal{W}, \gamma, \mathcal{Z})$ . Because h is soft conts, So  $h^{-1}(\mathcal{S}, E)$  is open<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Then  $g^{-1}(h^{-1}(\mathcal{S}, E))$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ . Since g is contra  $g^*\beta^s$ -conts. So  $(h \circ g)^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -closed in  $\mathcal{U}$ . Therefore  $h \circ g$  is contra  $g^*\beta^s$ -conts.

**Theorem 2.11.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -conts then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is soft conts.

**Proof.** Straightforward.

**Definition 2.12.** A function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is soft contra  $g^*\beta$  -irresolute, denoted by contra  $g^*\beta^s$  -ir.solute, if  $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$  for each  $g^*\beta^s$ -open in  $(\mathcal{S}, E)$  in  $(\mathcal{V}, \mu, \mathcal{K})$ .

**Theorem 2.13.** If a function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$  -irresolute and  $\mathcal{U}$  be a  $g^*\beta^s$  - lc.indisc, then g is soft contra conts. **Proof.** Obvious.

**Theorem 2.14.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$  -ir.solute and

 $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is soft conts then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -conts.

**Proof.** Let  $(\mathcal{S}, E)$  be closed<sup>s</sup> in  $(\mathcal{W}, \gamma, \mathcal{Z})$ . As h is soft conts then  $h^{-1}(\mathcal{S}, E)$  is closed<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Then  $g^{-1}(h^{-1}(\mathcal{S}, E))$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ . Since g is contra  $g^*\beta^s$ -ir.solute. So  $(h \circ g)^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -open in  $\mathcal{U}$ . Therefore  $h \circ g$  is contra  $g^*\beta^s$ -conts.

**Theorem 2.15.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -ir.solute and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -conts then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -conts.

**Proof.** Let  $(\mathcal{S}, E)$  be closed<sup>s</sup> in  $(\mathcal{W}, \gamma, \mathcal{Z})$ . As h is contra  $g^*\beta^s$ -conts then  $h^{-1}(\mathcal{S}, E)$  is closed<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Since g is contra  $g^*\beta^s$ -ir.solute, then  $g^{-1}(h^{-1}(\mathcal{S}, E))$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Therefore  $h \circ g$  is contra  $g^*\beta^s$ -conts.

**Theorem 2.16.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  contra  $g^*\beta^s$  -ir.solute and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -ir.solute then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is contra  $g^*\beta^s$ -ir.solute.

**Proof.** Let  $(\mathcal{S}, E)$  be closed<sup>s</sup> in  $(\mathcal{W}, \gamma, \mathcal{Z})$ . As h is contra  $g^*\beta^s$ -ir.solute, then  $h^{-1}(\mathcal{S}, E)$  is closed<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Since g is contra  $g^*\beta^s$ -ir.solute, then  $g^{-1}(h^{-1}(\mathcal{S}, E))$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Therefore  $h \circ g$  is contra  $g^*\beta^s$ -ir.solute.

**Theorem 2.17.** Let  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  be a two functions in STS such that  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$ 

- 1. If g is contra  $g^*\beta^s$ -ir.solute and h is contra  $g^*\beta^s$ -conts, then  $h \circ g$  is contra  $g^*\beta^s$ -conts.
- 2. If g is  $g^*\beta^s$ -ir.solute and h is contra  $g^*\beta^s$ -ir.solute, then  $h \circ g$  is contra  $g^*\beta^s$ -ir.solute.

**Proof.** Obvious.

#### 3. Soft Almost Contra $g^*\beta$ - Continuous Function

**Definition 3.1.** A function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is soft almost contra  $g^*\beta$ continuous, denoted by Alm.contra  $g^*\beta^s$ -conts, if  $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ for each soft regular open (briefly,  $r^s$ -open) in  $(\mathcal{V}, \mu, \mathcal{K})$ .

**Theorem 3.2.** If  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  contra  $g^*\beta^s$ -conts then it is Alm.contra  $g^*\beta^s$ -conts.

**Proof.** Since every  $r^s$ -open set is open set.

**Theorem 3.3.** Let  $g: (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  be a function then every  $g^*\beta^s$ -ir.solute continuous is Alm.contra  $g^*\beta^s$ -conts.

**Theorem 3.4.** A function  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$ , then the following conditions are equivalent.

(a) g is Alm.contra  $g^*\beta^s$ -conts.

(b) The inverse image of each  $r^s$ - closed in  $(\mathcal{V}, \mu, \mathcal{K})$  is  $g^*\beta^s$ -open.

**Proof.**  $(a) \Rightarrow (b)$ : Let  $(\mathcal{S}, E)$  is  $r^s$ - closed in  $(\mathcal{V}, \mu, \mathcal{K})$ . Thus  $\mathcal{V} - (\mathcal{S}, E)$  is  $r^s$ -open set in  $(\mathcal{V}, \mu, \mathcal{K})$ . Hence by  $(a), g^{-1}(\mathcal{V} - (\mathcal{S}, E)) = \mathcal{U} - g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ . Therefore  $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$  $(b) \Rightarrow (a)$ : Let  $(\mathcal{S}, E)$  is  $r^s$ - open in  $(\mathcal{V}, \mu, \mathcal{K})$ . Thus  $\mathcal{V} - (\mathcal{S}, E)$  is  $r^s$  closed set in  $(\mathcal{V}, \mu, \mathcal{K})$ . Hence by  $(b), g^{-1}(\mathcal{V} - (\mathcal{S}, E)) = \mathcal{U} - g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Therefore

 $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ .

**Theorem 3.5.** If  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is Alm. contra  $g^*\beta^s$ -cont and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is  $r^s$ -set connected, then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is Alm. contra  $g^*\beta^s$ -cont and Alm.  $g^*\beta^s$ -conts

**Proof.** Let  $(\mathcal{S}, E)$  is  $r^s$  open in  $\mathcal{W}$ . As h is  $r^s$ -connected set, then  $h^{-1}(\mathcal{S}, E)$  is clopen<sup>s</sup> in  $(\mathcal{V}, \mu, \mathcal{K})$ . Since g is Alm.contra  $g^*\beta^s$ -conts, then  $g^{-1}(h^{-1}(\mathcal{S}, E))$  is  $g^*\beta^s$ -open and  $g^*\beta^s$ -closed in  $(\mathcal{U}, \tau, E)$ . Therefore  $h \circ g$  is Alm.contra  $g^*\beta^s$ -conts and Alm  $g^*\beta^s$ -conts.

**Theorem 3.6.** If  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is contra  $g^*\beta^s$ -conts and  $h : (\mathcal{V}, \mu, \mathcal{K}) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is  $r^s$ -set connected, then  $h \circ g : (\mathcal{U}, \tau, E) \to (\mathcal{W}, \gamma, \mathcal{Z})$  is  $g^*\beta^s$  conts and  $Alm.g^*\beta^s$ -conts. **Proof.** Obvious.

**Theorem 3.7.** If  $g : (\mathcal{U}, \tau, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is an Alm.contra  $g^*\beta^s$ -conts and  $(\mathcal{H}, E)$  is open<sup>s</sup> subset of  $\mathcal{U}$ , then the restriction  $g/(\mathcal{H}, E) : (\mathcal{H}, E) \to (\mathcal{V}, \mu, \mathcal{K})$  is Alm.contra  $g^*\beta^s$ -conts.

**Proof.** Let  $(\mathcal{S}, E)$  is  $r^s$ - closed in  $\mathcal{V}$ . Because g is Alm.contra  $g^*\beta^s$ -conts,  $g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -open in  $(\mathcal{U}, \tau, E)$ . Since  $(\mathcal{H}, E)$  is open<sup>s</sup>. Hence  $(g/(\mathcal{H}, E))^{-1}(\mathcal{S}, E) = (\mathcal{H}, E) \cap g^{-1}(\mathcal{S}, E)$  is  $g^*\beta^s$ -open in  $(\mathcal{H}, E)$ . Thus  $g/(\mathcal{H}, E)$  is Alm.contra  $g^*\beta^s$ -conts.

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