

## EXTENDED VALUES OF RAMANUJAN'S TAU FUNCTION

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*Dedicated to Professor G.E. Andrews on his seventieth birthday*

**Abstract:** Present paper concerns mainly with verification and extension of table for  $\tau(1), \tau(2), \tau(3), \tau(4), \dots, \tau(29), \tau(30)$  of Ramanujan. Our extended table for  $\tau(31), \tau(32), \dots, \tau(37)$  is obtained without using certain arithmetical functions defined by Ramanujan and also the theory of elliptic functions.

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### 1. Introduction

In this paper, we obtain the values of  $\tau(31), \tau(32), \tau(33), \tau(34), \tau(35), \tau(36)$  and  $\tau(37)$ , where  $\tau(n)$  is Tau function of Ramanujan, defined as follows:

$$\sum_{n=1}^{\infty} \tau(n) x^n = x \left\{ \prod_{n=1}^{\infty} (1 - x^n) \right\}^{24} \quad (1.1)$$

Ramanujan [3, p.196, Table(V); see also 1,2] calculated the values of  $\tau(1), \tau(2), \tau(3), \tau(4), \dots, \tau(29), \tau(30)$ , by means of the theory of elliptic functions and certain arithmetical functions such as  $F_{r,s}(x)$ ,  $\Phi_{r,s}(x)$ ,  $E_{r,s}(n)$ ,  $\sigma_s(n)$ , Riemann's Zeta function  $\zeta(n)$ , greatest integer function  $[x]$ , theory of symbols  $o, O$ , continued fraction, asymptotic expansion, some trigonometrical identities, inequalities, Gamma function, theory of order of error terms, number theory, convergence and divergence of infinite series.

We have obtained the values of  $\tau(1), \tau(2), \tau(3), \tau(4), \dots, \tau(36), \tau(37)$  without using the theory of elliptic functions and certain arithmetical functions etcetera. In this sequence, we consider the whole square of power series  $\sum_{n=0}^{\infty} b_n x^n$  and collect the terms upto  $x^{36}$ . Thus we have: