

A CERTAIN CLASS OF MULTIPLE GENERATING FUNCTIONS INVOLVING MITTAG-LEFFLER'S FUNCTIONS

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Abstract: A set of certain class of multiple generating function involving Mittag-Leffler's functions E_{α} , $E_{\alpha,\beta}$ and related function $\phi(\alpha,\beta;z)$ of wright is given. Some interesting (known and new) multiple generating functions are also obtained as special cases.

Key Words : Mittag-Leffler's functions and related functions and related function, Bessel's function and Hyper-Bessel function, Hypergeometric function.

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1. Introduction and Definition

In the usual notation, let ${}_pF_q$ denote a generalized hypergeometric function of one variable with p and q parameters (positive integer or zero), defined by [6; p.42(1)].

$$\begin{aligned} {}_pF_q \left[\begin{matrix} a_1, a_2, \dots, a_p; \\ b_1, b_2, \dots, b_q \end{matrix} ; z \right] &= \sum_{n=0}^{\infty} \frac{(a_1)_n (a_2)_n \dots (a_p)_n z^n}{(b_1)_n (b_2)_n \dots (b_q)_n n!} \\ &= {}_pF_q [a_1, \dots, a_p; b_1, \dots, b_q; z] \end{aligned} \quad (1.1)$$

(by $\neq 0, -1, -2, \dots, j=1, 2, \dots, q$)