

## DOUBLE ROMAN DOMINATION NUMBER OF MIDDLE GRAPH

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**Abstract:** For any graph  $G(V, E)$ , a function  $f : V(G) \rightarrow \{0, 1, 2, 3\}$  is called Double Roman dominating function (DRDF) if the following properties holds,

1. If  $f(v) = 0$ , then there exist two vertices  $v_1, v_2 \in N(v)$  for which  $f(v_1) = f(v_2) = 2$  or there exist one vertex  $u \in N(v)$  for which  $f(u) = 3$ .
2. If  $f(v) = 1$ , then there exist one vertex  $u \in N(v)$  for which  $f(u) = 2$  or  $f(u) = 3$ .

The weight of DRDF is the value  $w(f) = \sum_{v \in V(G)} f(v)$ . The minimum weight among all double Roman dominating function is called double Roman domination