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SOME SPECIAL FAMILIES OF HOLOMORPHIC AND AL-OBOUDI TYPE BI-UNIVALENT FUNCTIONS ASSOCIATED WITH (m,n)-LUCAS POLYNOMIALS INVOLVING MODIFIED SIGMOID ACTIVATION FUNCTION

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Abstract: The aim of the present paper is to introduce some special families of holomorphic and Al-Oboudi type bi-univalent functions associated with (m, n)-Lucas polynomials involving modified sigmoid activation function $\phi(s) = \frac{2}{1+e^{-s}}, s \ge 0$ in the open unit disc \mathfrak{D} . We investigate the upper bounds on initial coefficients for functions of the form $g_{\phi}(z) = z + \sum_{j=2}^{\infty} \phi(s) d_j z^j$, in these newly introduced special families and also discuss the Fekete-Szegö problem. Some interesting consequences of the results established here are also indicated.

Keywords and Phrases: Holomorphic function, Bi-univalent function, Fekete - Szegö inequality, (m, n)-Lucas polynomials, Modified sigmoid function.

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