

SOME SPECIAL SETS IN AN EXPONENTIAL VECTOR SPACE

Priti Sharma and Sandip Jana*

Department of Mathematics,
Bangabasi College, University of Calcutta,
19, Rajkumar Chakraborty Sarani, Kolkata - 700009, INDIA

E-mail : mspriti23@gmail.com

*Department of Pure Mathematics,
University of Calcutta,
35, Ballygunge Circular Road, Kolkata - 700019, INDIA

E-mail : sjpm@caluniv.ac.in

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Abstract: In this paper, we have studied ‘absorbing’ and ‘balanced’ sets in an Exponential Vector Space (*evs* in short) over the field \mathbb{K} of real or complex numbers. We have characterised a local base at the additive identity in terms of balanced and absorbing sets in a topological *evs* over the field \mathbb{K} . We have introduced the concept of ‘bounded sets’ in a topological *evs* over the field \mathbb{K} and characterised them with the help of balanced sets. Finally we have introduced the concept of ‘radial’ *evs* which characterises an *evs* over the field \mathbb{K} up to order-isomorphism. It has been shown that “the usual subspace topology is the finest topology with respect to which $[0, \infty)$ forms a topological *evs* over the field \mathbb{K} ”.

Keywords and Phrases: Topological exponential vector space, order-isomorphism, absorbing set, balanced set, bounded set, radial *evs*.

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1. Introduction

Exponential vector space is a new algebraic structure consisting of a semigroup, a scalar multiplication and a compatible partial order which can be thought of as an