South East Asian J. of Mathematics and Mathematical Sciences Vol. 16, No. 1 (2020), pp. 111-122

ISSN (Online): 2582-0850

ISSN (Print): 0972-7752

SOME HYPERGEOMETRIC GENERATING FUNCTIONS MOTIVATED BY THE WORK OF BEDIENT AND RAINVILLE

M. I. Qureshi and Bilal Ahmad Bhat

Department of Applied Sciences and Humanities, Faculty of Engineering and Technology, Jamia Millia Islamia (A Central University), New Delhi -110025, INDIA

E-mail: miqureshi_delhi@yahoo.co.in, bilalj102102@gmail.com

(Received: Oct. 11, 2019 Accepted: Feb. 24, 2020 Published: Apr. 30, 2020)

Abstract: In this article, some hypergeometric generating relations involving Kampé de Fériet's double hypergeometric functions are derived by using series rearrangement technique, a reduction formula and Whipple's quadratic transformation. Some special cases involving Appell's functions of second, third kind, Rainville polynomial and two Bedient's polynomials, are also obtained.

Keywords and Phrases: Hypergeometric functions, Series rearrangement technique, Whipple's quadratic transformation, Bedient polynomials.

2010 Mathematics Subject Classification: 33C20, 33C45, 05A15.

1. Introduction and Preliminaries

In our investigations, we shall use the following standard notations: $\mathbb{N} := \{1,2,3,\cdots\}; \mathbb{N}_0 := \mathbb{N} \bigcup \{0\}; \mathbb{Z}_0^- := \mathbb{Z}^- \bigcup \{0\} = \{0,-1,-2,-3,\cdots\}.$ The symbols $\mathbb{C}, \mathbb{R}, \mathbb{N}, \mathbb{Z}, \mathbb{R}^+$ and \mathbb{R}^- denote the sets of complex numbers, real numbers, natural numbers, integers, positive and negative real numbers, respectively. The Pochhammer symbol $(\alpha)_p(\alpha, p \in \mathbb{C})[12, p.22 \text{ Eq.}(1), p.32, Q.N.(8) \text{ and } Q.N.(9)],$ see also [13, p.23, Eq.(22) and Eq.(23)] is defined by

$$(\alpha)_p = \frac{\Gamma(\alpha + p)}{\Gamma(\alpha)}$$