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## FEKETE-SZEGÖ TYPE COEFFICIENT INEQUALITIES FOR CERTAIN SUBCLASSES OF ANALYTIC FUNCTIONS

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**Abstract:** In the present investigation, the authors obtain Fekete-Szegö inequality for certain subclasses of analytic functions on the open unit disk. For these classes, the Fekete-Szegö type defined through fractional derivatives is obtained.

**Keywords and Phrases:** Univalent functions, starlike functions, convex functions, subordination, Fekete-Szegö inequalities.

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## 1. Introduction

Let  $\mathcal{M}$  denote the class of all analytic functions which are analytic in the unit disk  $\Delta = \{z : z \in \mathbb{C}, |z| < 1\}$  of the form

$$f(z) = z + \sum_{j \ge 2} a_j z^j,$$
 (1.1)

and S be the subclass of  $\mathcal{M}$  consisting of univalent functions. Let  $\Phi(z)$  be an analytic function with positive real part on  $\Delta$  with  $\Phi(0) = 1$ ,  $\Phi'(0) > 0$  and  $Re \ \Phi(z) > 0$   $(z \in \Delta)$  which maps the unit disc  $\Delta$  onto a starlike region with