

ON CONTINUED FRACTIONS AND LAMBERT SERIES

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Dedicated to Prof. K. Srinivasa Rao on his 75th Birth Anniversary

Abstract: In this paper, we have established certain results involving continued fractions and Lambert series.

Keywords and Phrases: Lambert series, continued fractions, q-shifted factorial, basic hypergeometric series.

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1. Introduction, Notations and Definitions

The q-shifted factorial is defined by,

$$(a; q)_n = \begin{cases} 1, & n = 0 \\ (1-a)(1-aq)\dots(1-aq^{n-1}), & n \geq 1 \end{cases}$$

Also,

$$(a; q)_{-n} = \frac{q^{n(n+1)/2}}{(-a)^n (q/a; q)_n}$$

The generalized basic hypergeometric series is given by,

$${}_r\Phi_{r-1} \left[\begin{matrix} a_1, a_2, \dots, a_r; q; z \\ b_1, b_2, \dots, b_{r-1} \end{matrix} \right] = \sum_{n=0}^{\infty} \frac{(a_1; q)_n (a_2; q)_n \dots (a_r; q)_n z^n}{(b_1; q)_n (b_2; q)_n \dots (b_{r-1}; q)_n (q; q)_n},$$

where $\max. (|q|, |z|) < 1$.

A generalized bilateral basic hypergeometric series is defined by,

$${}_r\Psi_r \left[\begin{matrix} a_1, a_2, \dots, a_r; q; z \\ b_1, b_2, \dots, b_r \end{matrix} \right] = \sum_{n=-\infty}^{\infty} \frac{(a_1; q)_n (a_2; q)_n \dots (a_r; q)_n z^n}{(b_1; q)_n (b_2; q)_n \dots (b_r; q)_n},$$